

# 3D Targets for Evaluating Fingerprint Readers

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**Abstract**—Standard calibration targets are typically used for calibrating the imaging pathway of fingerprint readers. However, there is no standard method for evaluating fingerprint readers in the operational setting where variations in finger placement by the user are encountered. The goal of this research is to design 3D targets for repeatable operational evaluation of fingerprint readers. 2D calibration patterns with known characteristics (e.g. sinusoidal gratings of pre-specified orientation and frequency, synthetic fingerprints with known singular points and minutiae) are projected onto a generic 3D finger surface to create electronic 3D targets. A state-of-the-art 3D printer (Stratasys Objet350 Connex) is used to fabricate the 3D targets with material similar in hardness and elasticity to the human finger skin. Our experimental results show that the (i) fabricated 3D targets can be imaged using three different (500/1000 ppi) commercial optical fingerprint readers, (ii) salient features in the 2D calibration patterns are preserved during the synthesis and fabrication of 3D targets, and (iii) intra-class variability between multiple impressions of the 3D targets captured using the optical fingerprint readers does not degrade the recognition accuracy. We also conduct experiments to demonstrate that the fabricated 3D targets can be used for operational evaluation of fingerprint readers.

**Keywords**—3D targets, fingerprint reader evaluation, 2D calibration patterns, 3D printing, 2D pattern to 3D surface projection.

## 1 INTRODUCTION

CALIBRATION of imaging systems typically involves the use of specially designed objects with known properties, called *calibration targets*. In the biomedical domain, for instance, such objects (called *phantoms*) are used for calibrating and testing optical measurement profiles of sensing instrumentation [2], [3]. Similarly, calibration targets (Fig. 1) are also used for calibrating fingerprint readers.

There are two separate standards currently in use by the Federal Bureau of Investigation (FBI) for the certification of fingerprint readers, (i) the *PIV-071006*, which caters to single finger readers designed for applications involving person verification (one-to-one comparison), and (ii) the *Appendix F*, which applies to fingerprint readers designed for use in large scale applications involving person identification (one-to-many comparisons). The *Appendix F* standard has more stringent image quality requirements compared to the *PIV-071006* standard [5]. To get their readers certified, fingerprint vendors need to demonstrate that the images captured using their readers meet the image quality specifications laid out in the relevant standard [4] [6]. A typical procedure is (i) to use 2D/3D calibration targets to ascertain if the images of

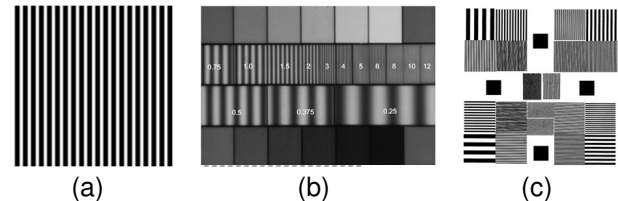


Fig. 1. 2D images of targets used for calibrating fingerprint readers, (a) ronchi (vertical bar) target for calibrating the geometric accuracy, (b) sine wave target for measuring the resolution, and (c) multiple bar target for estimating the spatial frequency response of a fingerprint reader (images taken from [4]).

the targets captured using the reader meet the standard specifications, (ii) modify the reader configuration, if needed, to ensure it captures images of sufficient quality to meet the specifications, and (iii) when satisfied with the reader configuration, submit test images to the testing agency for review<sup>1</sup> [5]. Furthermore, the testing agency reviews the test data to verify that the submitted images meet the image quality specifications. If the test data is found to meet the desired specifications, the testing agency certifies the fingerprint reader as being compliant with the specific standard.

The testing and certification of biometric devices for use by Unique Identification Authority of India (UIDAI) in the Aadhaar project in India is performed by the Standardization Testing and Quality Certification (STQC)

1. Review of the submitted test data is conducted by the Technology Evaluation Standards Test Unit, Biometric Center of Excellence (BCOE) led by the Criminal Justice Information (CJI) Services Division [7].

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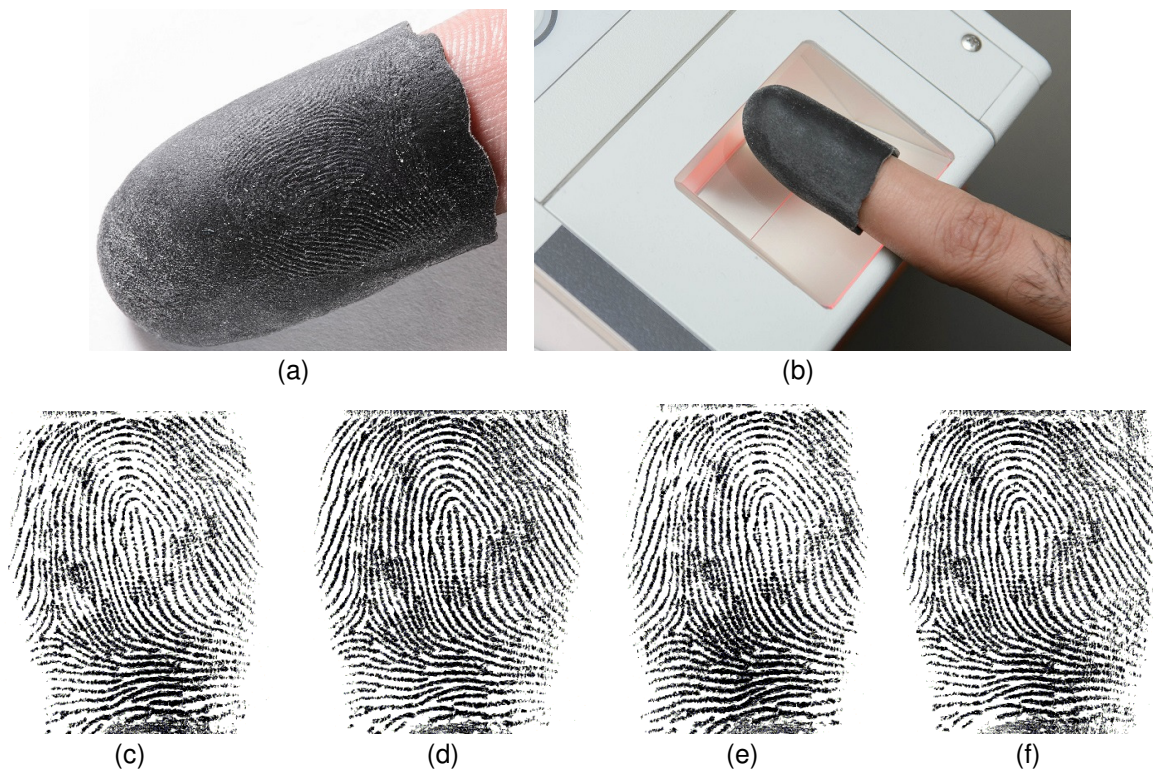


Fig. 2. Evaluating an optical fingerprint reader using the 3D targets designed and fabricated by the authors. (a) The 3D target is worn on a finger, (b) the finger is repeatedly placed on the fingerprint reader platen, and (c)-(f) multiple 2D impressions (four shown here) of the 3D target are captured which are utilized for evaluation of the reader.

Directorate, Government of India [8]. UIDAI is one of the largest consumers of biometric readers in the world, with currently, there being 36,000 enrolment stations deploying 11 different certified biometric readers in Aadhaar [9]. Image acquisition requirements equivalent to Appendix F are mandated for fingerprint readers used for enrolment in Aadhaar [10]. For getting their readers certified, fingerprint vendors submit a certification agreement to the certification agency, the STQC Directorate. The certification agency evaluates the evidence of conformity of the submitted agreement to the certification procedure guidelines. Thereafter, the STQC directorate tests the fingerprint reader in the lab to determine if it meets the standard specifications. Provided that the testing procedure results are satisfactory, the fingerprint reader is certified by the agency for use in Aadhaar [11].

Standard calibration targets can be used for calibrating the imaging pathway of a fingerprint reader. For example, the targets in [15] can be utilized for testing the frustrated total internal reflection (FTIR) pathway of an optical fingerprint reader. However, they cannot be used to evaluate a fingerprint reader for variations encountered operationally during the fingerprint capture process, e.g., application of different finger pressure on the reader platen, and placement of the finger in different ways by the user. This is because these targets are not

specifically fabricated using materials similar in properties to the human finger skin. Hence, it is not possible to mimic the typical fingerprint acquisition scenario using these targets, which involves the placement of finger with certain pressure on the fingerprint reader.

For operational evaluation of a fingerprint reader, one possibility, therefore, is to conduct pilot studies in the field using the fingerprint reader. This, however, is a tedious process both in terms of time and resource commitment, and is limited by the amount and nature of data collected. Besides, such a procedure cannot be used for repeatable operational evaluation of the fingerprint reader because, in practice, the same set of subjects is typically not available for repeated testing. The goal of this research, therefore, is to fabricate standard 3D targets which can be used for repeatable operational evaluation of fingerprint readers. We fabricate 3D targets with material similar in hardness and elasticity to the human finger skin specifically such that they can be worn on a finger and placed on the fingerprint reader platen in a natural manner (see Fig. 2).

The utility of the fabricated 3D targets extends beyond evaluation of fingerprint readers. 3D targets created by projecting 2D synthetic fingerprint images with known fingerprint features (e.g. type, minutiae and singular point locations) onto the 3D finger surface can be used

TABLE 1  
Comparison of existing fingerprint system evaluation methods with the proposed 3D target creation method

| Method            | Artifacts                              | Fingerprint Features   | Evaluation Use Cases   |
|-------------------|--|--|--|
| SFinGe [12]       | 2D synthetic fingerprints (electronic) | Known fingerprint ridge flow and ridge density features; uncontrolled minutiae placement     | Fingerprint feature extractors and matchers  |
| IBG DHS SBIR [13] | 2D synthetic fingerprints (electronic) | Known fingerprint ridge flow, ridge density features; partially controlled minutiae features | Fingerprint feature extractors and matchers  |
| Zhao et al. [14]  | 2D synthetic fingerprints (electronic) | Known fingerprint ridge flow, ridge density and minutiae features                            | Fingerprint feature extractors and matchers  |
| Proposed          | 3D targets (electronic and physical)   | Known fingerprint ridge flow, ridge density and minutiae features                            | End-to-end fingerprint systems, including fingerprint readers, feature extractors and matchers |

to evaluate fingerprint feature extraction and matching algorithms. Such targets can, therefore, be used for end-to-end evaluation of a fingerprint recognition system from placing the finger on the reader and capturing the 2D impression to extracting features and matching the captured image to the gallery templates. This is better than the existing methods which only use 2D synthetic fingerprint images for evaluation purposes (see Table 1).

A physical 3D target is created by projecting an electronic 2D calibration pattern onto a generic electronic 3D model of the finger surface<sup>2</sup>. The electronic 3D finger surface is first aligned such that the finger length is along the y-axis, width along the x-axis and depth along the z-axis. The electronic 3D finger surface is then preprocessed to ensure sufficient fidelity for approximately determining the correspondences between the electronic 2D calibration pattern and the electronic 3D finger surface. The electronic 2D calibration pattern is then mapped onto the front portion of the electronic 3D finger surface and correspondences between each vertex on the frontal electronic 3D surface and the pixel locations in the electronic 2D calibration pattern are established. The electronic 2D calibration pattern is engraved onto the frontal electronic 3D finger surface by displacing each vertex along the surface normal according to the texture values at the mapped pixel locations. Finally, the electronic 3D finger surface is post-processed to create an electronic model of a wearable 3D target ready for 3D printing.

The physical 3D targets are fabricated using a state-of-the-art 3D printer (Stratasys Objet350 Connex<sup>3</sup>) with material similar in hardness and elasticity to the human finger skin. The targets are imaged using three different (500/1000 ppi) commercial optical fingerprint readers. Our experimental results show that the captured images of the physical 3D targets can be successfully matched to the electronic 2D synthetic fingerprint patterns used to generate the 3D targets using a commercial fingerprint

SDK [17]. This demonstrates that the salient features present in the electronic 2D calibration pattern are essentially preserved when mapping it to the physical 3D surface of the fingerprint target. Experiments are also conducted to demonstrate that the intra-class variability between the different images of the 3D targets captured using the three optical readers is minimal. We also conduct experiments for operational evaluation of the three aforementioned optical fingerprint readers using the fabricated 3D targets.

## 2 SYNTHESIZING 3D TARGETS

A 3D target  $A$  is synthesized from a 2D calibration pattern  $I$  with pre-specified features, and a generic 3D finger surface  $S$ . Let the texture feature value in the 2D calibration pattern  $I$  at spatial coordinates  $(u, v)$  be denoted by  $I(u, v)$ . Also, assume that the 3D finger surface  $S$  is a triangular mesh having a set of vertices  $V$  and triangles  $T$ . Each vertex,  $v$ , in  $V$  has  $(x, y, z)$  coordinates corresponding to its spatial location in  $S$ , and a triangle in  $T$  connects a unique set of three vertices. Synthesizing the 3D target  $A$  using  $I$  and  $S$  then consists of the following steps (Fig. 3) (details of the processes summarized below are given in Sections 2.1-2.6):

- 1) **Preprocessing 3D finger surface:** Align  $S$  such that the finger length is along the y-axis in  $S$ . Sample vertices from the set  $V$  based on the curvature of  $S$ . This sampling process reduces the density of  $S$ , therefore, subdivide  $S$  (as explained in Section 2.1) to ensure sufficient fidelity during projection of the 2D calibration pattern  $I$ . Displace  $S$  outwards along the direction of the surface normals computed at each vertex to create an outer finger surface  $S_O$ . Separate the front  $S_{OF}$  and rear portion  $S_{OR}$  of  $S_O$  (see Fig. 4). The front portion  $S_{OF}$  of  $S_O$  will be used for projection. Retain the original surface  $S$ .
- 2) **Preprocessing 2D calibration pattern:** If the pattern  $I$  being projected is a 2D fingerprint image, extract the skeleton  $I_S$  of the image  $I$ . Increase the ridge width of the skeleton  $I_S$  using morphological operations, and smooth the image using a Gaussian filter before projecting it onto the

2. The 3D finger surface could either be the shape of the finger sensed using a 3D fingerprint scanner or a synthetically generated surface describing the shape of the finger. In our case, the finger surface was scanned using the Artec Eva 3D scanner [16].

3. The naming of companies and products does not imply endorsement or recommendation of those companies or products by the authors or the organizations they represent.

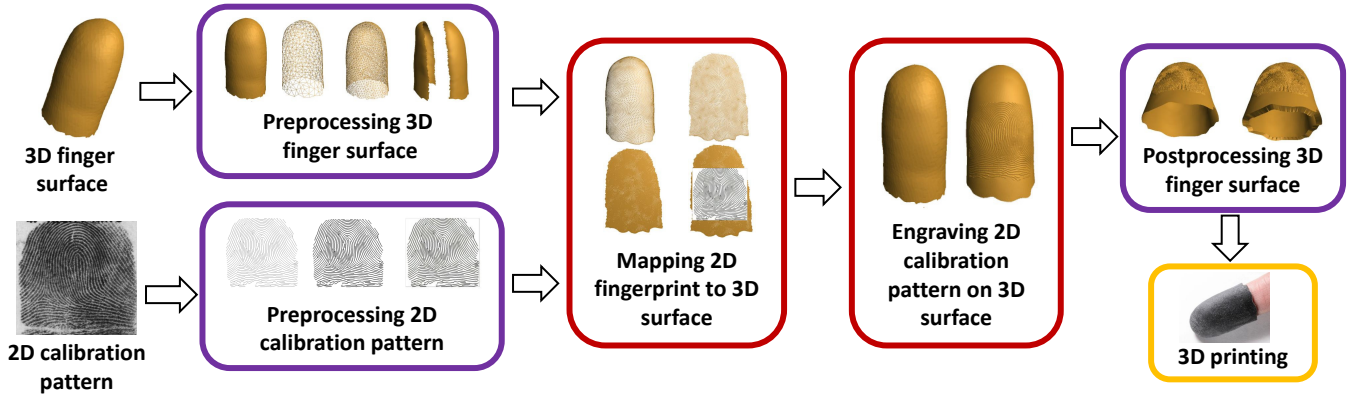


Fig. 3. Synthesizing a 3D target from a 2D calibration pattern and a 3D finger surface.

electronic frontal surface  $S_{OF}$ . This preprocessing step is necessary to ensure that ridges and valleys present in  $I$  are engraved smoothly onto  $S_{OF}$ . Note that this preprocessing step is not needed if any other 2D calibration pattern (e.g. sine grating) is being projected.

- 3) **Mapping 2D fingerprint to 3D surface:** Project the front portion  $S_{OF}$  of 3D finger surface  $S_O$  to 2D and correct for rotation and flip using corresponding control points between 3D surface  $S_{OF}$  and the 2D projection of  $S_{OF}$ , and translation with respect to reference coordinates computed from  $I$ . Make the front portion of the outer finger surface  $S_O$  dense depending on the resolution of  $I$  to ensure sufficient fidelity of mapping  $I$ . Determine the mapping between the  $(x, y, z)$  spatial locations of the vertices on the front portion of the outer 3D surface  $S_O$  and the  $(u, v)$  image domain of  $I$ .
- 4) **Engraving 2D calibration pattern on 3D surface:** To create ridges and valleys, displace the vertices on the front portion of  $S_O$  along the surface normals according to the texture values in  $I$  at the mapped  $(u, v)$  locations.
- 5) **Postprocessing 3D finger surface:** Combine the front and rear portions of the outer finger surface  $S_O$ . Make the original finger surface  $S$  as dense as the outer finger surface  $S_O$  and then stitch the two surfaces together to obtain a watertight solid target. This finishes the creation of the 3D target  $A$  as an electronic (virtual) target.
- 6) **3D Printing:** Specify the physical dimensions as well as the printing material according to the hardness and elasticity of the human finger skin before printing the 3D target  $A$  using a 3D printer (Stratasys Objet350 Connex).

A detailed description of each of these steps used in the 3D target creation process for a given 2D calibration pattern  $I$  and a 3D finger surface  $S$  is given below.

## 2.1 Preprocessing 3D finger surface

A sequence of preprocessing steps are executed on the 3D finger surface  $S$  before projecting the 2D calibration pattern  $I$  (see Fig. 4).

### Alignment

The 3D finger surface  $S$ , arbitrarily oriented in the  $(x, y, z)$  coordinate frame, is first aligned such that the finger length is along the  $y$ -axis, width along the  $x$ -axis and height on the  $z$ -axis. For doing this, each vertex in the set  $V$  is translated such that the center of the surface  $S$  coincides with the origin of the  $(x, y, z)$  coordinate axes. Principal component analysis (PCA) [18] is used to determine the principle directions of the surface spread. The computed principal components are then used to align the surface  $S$ . Note that this step only alters the absolute  $(x, y, z)$  coordinate values of the vertices in  $V$  and retains the geometry of the surface  $S$ .

### Remeshing

The 3D finger surface  $S$  is remeshed by sampling vertices from  $V$  using the method described in [19]. The first vertex  $v_1$  is sampled randomly from  $V$ , and the geodesic distance map  $U(v_1)$  from  $v_1$  to every other vertex in  $V$  is computed by solving the eikonal equation using the fast marching method [20]:

$$\|\Delta U(v_1)\| = P(v_1). \quad (1)$$

Here,  $\Delta$  is the gradient operator, and  $P = 1/F$ , where  $F$  is the speed of front propagation used in the fast marching method.

Vertices are then sampled iteratively by adding the farthest vertex among the remaining vertices in iteration  $i$  from the vertices in the sampled vertex set  $V_{i-1}$  at iteration  $i - 1$ . Note that the geodesic distance map  $U_i$ , at iteration  $i$ , is updated using the following equation:

$$U_i = \min(U_{i-1}, U(v_i)), \quad (2)$$

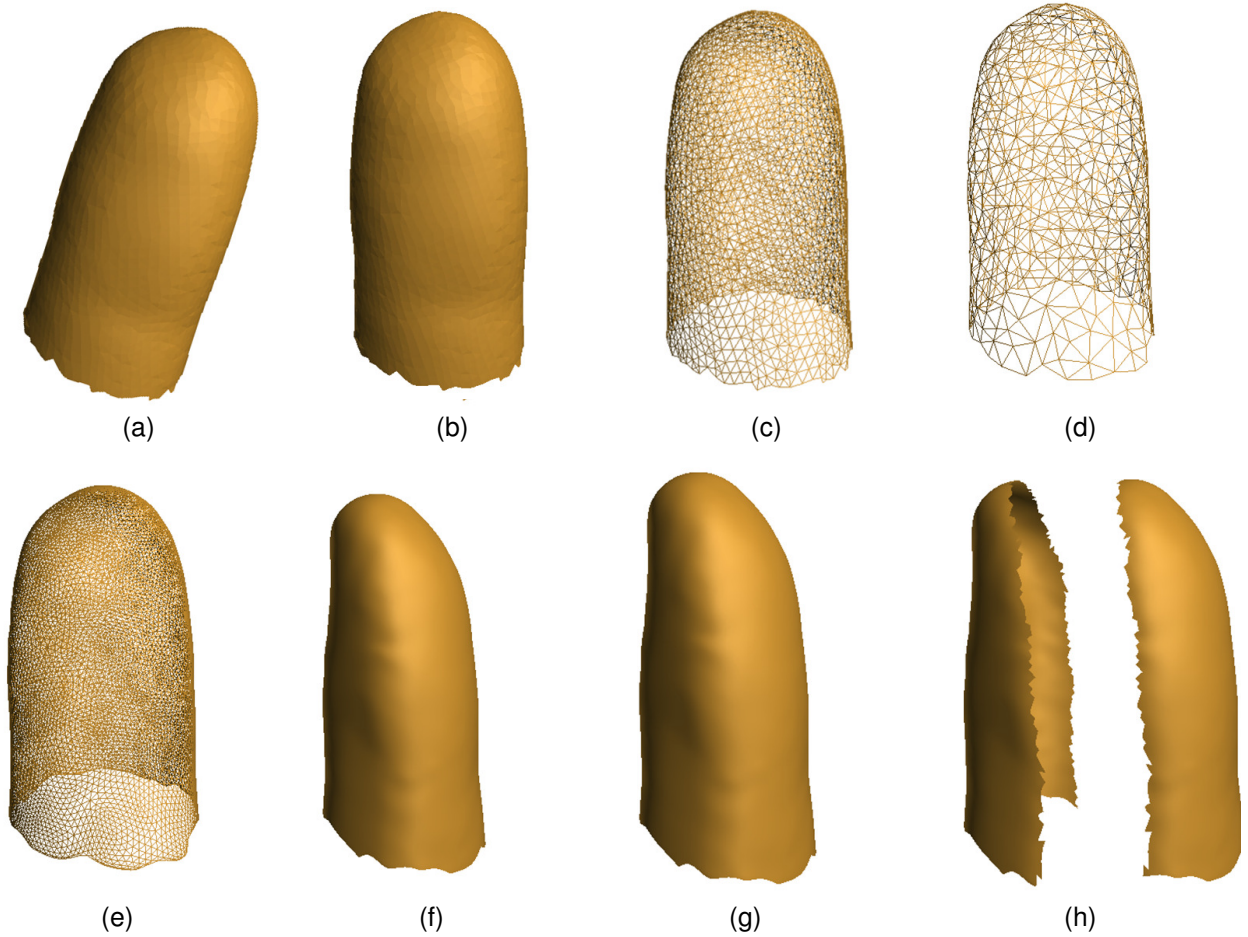


Fig. 4. Preprocessing 3D finger surface. (a) Original finger surface, (b) aligning the finger surface such that the finger length is along the y axis, (c) aligned finger surface (triangular mesh), (d) remeshing the finger surface (triangular mesh), (e) subdividing the surface (triangular mesh), (f) subdivided finger surface (profile view), (g) creating outer finger surface from (f), and (h) separating front and back portions of the outer finger surface.

where  $U(v_i)$  is the geodesic distance map of the vertex sampled at iteration  $i$ , and  $U_{i-1}$  is the geodesic distance map computed at iteration  $i - 1$ .

During this iterative procedure of sampling vertices, the speed of front propagation  $F$  is set to  $1/(1 + C)$ , where  $C$  is the aggregate curvature at each vertex in  $V$ . This results in more vertices being sampled in the higher curvature regions of the 3D surface and vice versa. The aggregate curvature  $C$  is calculated using the two principal curvatures  $C_{min}$  and  $C_{max}$  as follows,

$$C = |C_{min}| + |C_{max}|. \quad (3)$$

Here,  $|\cdot|$  is the absolute value operator,  $C_{min}$  and  $C_{max}$  are computed from the 3D curvature tensor  $T$  calculated using the method in [21]. In particular,  $C_{min}$  and  $C_{max}$  correspond to the two highest eigenvalues of the curvature tensor  $T$ .

Finally, Delaunay triangulation is used for reconstruct-

ing the remeshed surface from the set of sampled vertices [22].

### Subdivision

Although remeshing makes the surface  $S$  uniformly dense depending on its curvature, it reduces the surface density. To ensure sufficiently fidelity for projecting the 2D calibration pattern  $I$  onto the surface  $S$ , Loop's surface sub-division method [23] is used. Let the set of vertices and triangles obtained after remeshing be denoted by  $V_R$  and  $T_R$ , respectively. This method creates new vertices at each edge of every triangle in  $T_R$  using a weighted combination of neighborhood vertices, and creates new triangles by connecting the sampled vertices at edges adjacent to each other. The original vertices are then translated to maintain surface smoothness and continuity.



Fig. 5. Preprocessing a 2D fingerprint pattern before projection onto 3D finger surface. (a) Original fingerprint image, (b) extracted skeleton of the fingerprint in (a), (c) skeleton in (b) after applying the morphological operation of dilation, and (d) dilated skeleton in (c) smoothed using a gaussian filter.

### Creating outer surface

Let  $V_S$  and  $T_S$  be the set of vertices and triangles obtained after surface subdivision. Each vertex  $v$  in the set  $V_S$  is then displaced by a fixed factor  $d$  along the normal  $n$  computed at the vertex  $v$ :

$$\begin{bmatrix} v'_x \\ v'_y \\ v'_z \end{bmatrix} = \begin{bmatrix} v_x \\ v_y \\ v_z \end{bmatrix} + \begin{bmatrix} n_x \\ n_y \\ n_z \end{bmatrix} \times d \quad (4)$$

This is done to create an outer finger surface  $S_O$  where the 2D calibration pattern will be projected. The parameter  $d$  determines the thickness of the 3D target. Ideally, it is desirable to set  $d$  to be as small as possible. However, due to the limitation of the 3D printer resolution used for fabricating the targets, choosing a very small  $d$  results in the printed model being fragile. Therefore,  $d$  is empirically set to 1.5 mm in our experiments.

### Separating front and rear portions

Front and rear portions of the outer finger surface  $S_O$  are then separated by computing the surface normals at each triangle in  $T_S$ , and then retaining the triangles and corresponding vertices where surface normals have the z-component greater than 0 in the front surface, and the rest in the rear surface. Note that the alignment of the finger surface done in step 1) facilitates this separation process. Let us denote the front portion of the outer surface  $S_O$  as  $S_{OF}$  having the set of vertices  $V_{OF}$  and triangles  $T_{OF}$ . Similarly, let the rear portion be denoted as  $S_{OR}$  with the set of vertices  $V_{OR}$  and triangles  $T_{OR}$ . Also, note that we retain the original finger surface  $S$  having the set of vertices  $V_S$  and triangles  $T_S$ .

## 2.2 Preprocessing 2D calibration pattern

If the pattern  $I$  being projected is a fingerprint image, the following preprocessing steps are executed on  $I$ :

- 1) The skeleton of  $I$  is extracted using a commercial fingerprint SDK [17]. The skeleton is a 1-pixel wide ridge pattern. Let the skeleton be denoted by  $I_S$ .

- 2) The ridge width on the skeleton  $I_S$  is increased to 3 pixels by performing the morphological operation of dilation using a 2 pixel radius disk structured element.
- 3)  $I_S$  is filtered using a  $4 \times 4$  Gaussian filter with  $\sigma = 2.5$ . This is necessary to ensure that ridges and valleys present in the 2D fingerprint pattern  $I$  are engraved smoothly onto the 3D finger surface.

This preprocessing is not needed if any other calibration pattern (e.g. sine grating of certain orientation and frequency) is being projected.

## 2.3 Mapping 2D calibration pattern to 3D surface

The front portion  $S_{OF}$  of the outer finger surface  $S_O$  is projected from 3D  $((x, y, z)$  coordinate space) to 2D  $((u, v)$  coordinate space) by computing the ISOMAP embedding described in [24] (see Fig. 6). Recall that the vertices and triangles in  $S_{OF}$  are  $V_{OF}$  and  $T_{OF}$ , respectively. The ISOMAP embedding is computed by:

- 1) **Constructing adjacency graph:** An adjacency graph  $G$  is created, by connecting all vertex pairs  $\{v_i, v_j\}$  in  $V_{OF}$  that share an edge of any triangle in  $T_{OF}$ . The edge weights in  $G$  are set to the euclidean distance  $D(v_i, v_j)$  between the vertex locations. Note that for non-adjacent vertex pairs that do not share any edge,  $D$  is set to  $\infty$ .
- 2) **Computing shortest paths:** Dijkstra's shortest path algorithm [25] is used to compute the shortest path between all pairs of nodes in  $G$ . Geodesic distances between all pairs of vertices in  $V_{OF}$  are estimated by the shortest path distances of the nodes in  $G$ .
- 3) **Constructing 2D embedding:** Let the matrix  $D_G$  contain the shortest path distances computed in the previous step. Given  $D_G$ , classical multidimensional scaling (MDS) [26] is used to create the 2D embedding of vertices. MDS maintains the intrinsic geometry of the surface  $S_{OF}$  during the 3D to 2D projection.

ISOMAP embedding is used because it minimizes the distortion induced when projecting the front portion  $S_{OF}$

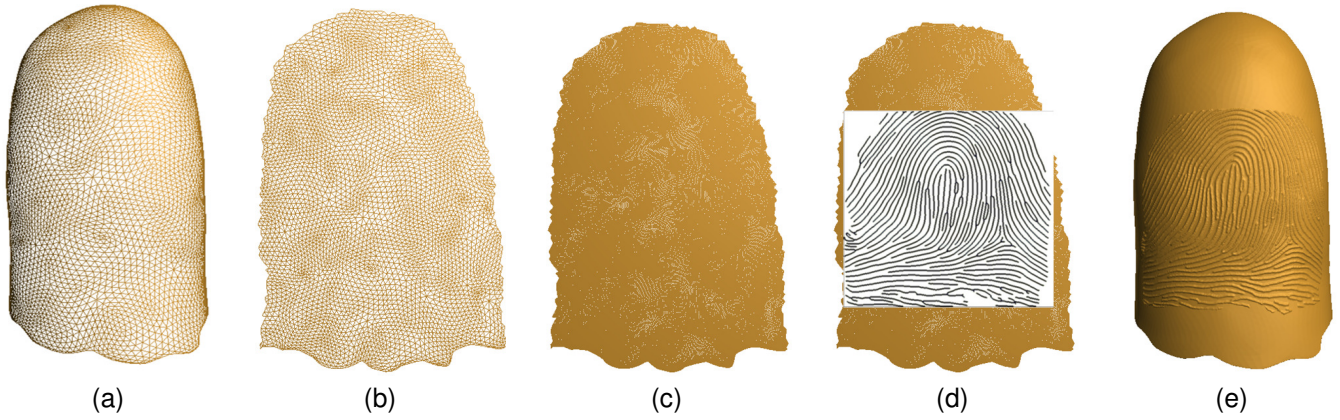


Fig. 6. Mapping and engraving a 2D calibration pattern onto the front portion of the outer 3D finger surface. (a) 3D frontal outer finger surface, (b) frontal surface in (a) is projected into 2D, (c) the 2D projected frontal surface is subdivided, (d) correspondences are determined between the 2D projected frontal finger surface and 2D calibration pattern, (e) 3D frontal outer finger surface in (a) is displaced along the surface normals to engrave the pattern.

of the 3D surface to 2D by preserving the geodesic distances between neighborhood vertices on  $S_{OF}$  during the 3D to 2D projection<sup>4</sup>.

Let the 2D projected frontal surface in the  $(u, v)$  coordinate space be denoted by  $S_{OFP}$  with the set of vertices  $V_{OFP}$  and the set of triangles  $T_{OFP}$ . Rotation and flip during the 3D to 2D projection of  $S_{OF}$  are corrected using corresponding control points between  $S_{OF}$  and  $S_{OFP}$ . Reference coordinates  $[r_u, r_v]$  are extracted from the 2D calibration pattern  $I$  for translation correction during the 3D to 2D projection of  $S_{OF}$ :

- If the pattern  $I$  being projected is a synthetic fingerprint image, then reference coordinates  $[r_u, r_v]$  are extracted from the fingerprint image using the method described in [27].
- If any other calibration pattern is being projected (e.g. sine gratings, horizontal/vertical bar patterns etc.) , then the location of the center pixel in the 2D calibration pattern  $I$  is used as the reference point i.e.  $[r_u, r_v] = [w/2, h/2]$ , where  $w$  and  $h$  are the width and height of the 2D pattern  $I$ .

The next step is to determine the one-to-one mapping between the pixel locations  $(u, v)$  on  $I$  and the vertices  $V_{OF}$  on  $S_{OFP}$ . For accurately determining the one-to-one correspondence, the density of  $S_{OF}$  as well as its 2D projection  $S_{OFP}$  is further increased using midpoint surface subdivision. Vertices are sampled on the midpoints of the edges in  $T_{OF}$ , and the sampled vertices on the adjacent edges are joined to create new triangles. The resolution of  $I$  being projected is factored into the computations while determining the correspondence between pixel locations on  $I$  and vertices  $V_{OF}$  on  $S_{OFP}$ . For example, if the

4. Discrete conformal mapping was used for projecting a 2D image to 3D finger surface in the earlier version of this paper [1]. It was, however, observed that discrete conformal mapping did not preserve the distances on the calibration pattern near the periphery of the 3D surface since it is an angle preserving mapping.

calibration pattern being projected has a resolution of 500 ppi, the scale of projection is 19.685 pixels/mm. Therefore, the coordinates of  $I$  are scaled by this factor before determining the correspondence.

Ideally, the density of  $S_{OF}$  needs to be increased according to the dimensions of the  $I$  being projected. For example, if a calibration pattern of width  $w$  and height  $h$  is being projected, then exactly  $w \times h$  vertices are required in the projection region for building the exact correspondence between the pixel locations on  $I$  and the vertices on  $S_{OF}$ . However, this is not recommended because it would result in a very large number of vertices and triangles on the surface and considerably increase the computational complexity of further processing on the surface. Therefore, the density of  $S_{OF}$  is only increased to a certain degree to retain the essential topology of the pattern being projected<sup>5</sup>. Let the set of vertices and triangles on the 2D projected frontal surface obtained after this step be denoted by  $V_{OFPS}$  and  $T_{OFPS}$ . The corresponding vertices and triangles on the outer 3D frontal surface be  $V_{OFS}$  and  $T_{OFS}$ , respectively. The one-to-one correspondence between the pixel locations on the calibration pattern  $I$  and the set of vertices  $V_{OFP}$  is then established.

## 2.4 Engraving 2D calibration pattern on 3D surface

In the penultimate step, surface normals are computed at each vertex in the set  $V_{OFPS}$ . The vertices are then displaced along their surface normals to engrave the fingerprint ridges and valleys on  $S_{OF}$  (see Fig. 6 (e)). Let the normal at a vertex  $v$  in the set  $V_{OFPS}$  be denoted by  $(n_x, n_y, n_z)$ , where  $n_x$ ,  $n_y$  and  $n_z$  represent the normal components along the  $x$ ,  $y$  and  $z$  directions, respectively.

5. For the finger surface used in our experiments, the density is increased so that there are approximately 250,000 vertices and 500,000 triangles on the front portion of the 3D surface.

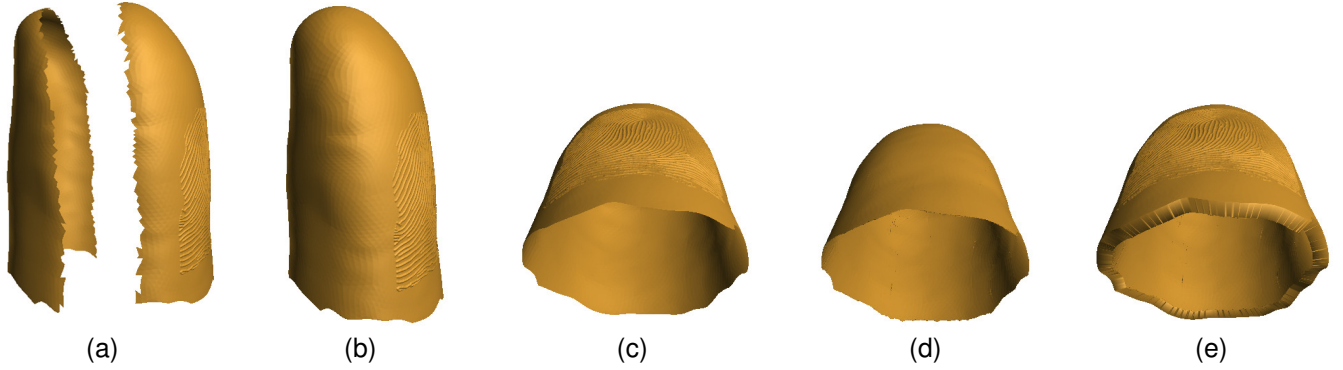


Fig. 7. Postprocessing 3D finger surface. (a) Separated front and rear portions of outer 3D surface, (b) front and rear portions shown in (a) are combined to create the outer 3D finger surface, (c) outer 3D finger surface (bottom view), (d) the retained original 3D finger surface (bottom view), (e) 3D electronic target created by stitching the outer and original surface in (c) and (d).

TABLE 2

Comparison of mechanical properties of the two different printing materials with the human finger skin.

| Property                | Human Skin<br>[29] [30] | TangoBlackPlus<br>FLX980 [31] | FLX 9840<br>-DM [32] |
|-------------------------|-------------------------|-------------------------------|----------------------|
| Shore A hardness        | 20-41                   | 26-28                         | 35-40                |
| Tensile Strength (MPa)  | 5-30                    | 0.8-1.5                       | 1.3-1.8              |
| Elongation at Break (%) | 35-115                  | 170-220                       | 110-130              |

The displaced coordinates of the vertex  $(v'_x, v'_y, v'_z)$  along the normal are then computed using the principle of vertex displacement mapping [28] as follows:

$$\begin{bmatrix} v'_x \\ v'_y \\ v'_z \end{bmatrix} = \begin{bmatrix} v_x \\ v_y \\ v_z \end{bmatrix} + \begin{bmatrix} n_x \\ n_y \\ n_z \end{bmatrix} \times (1 - I'(u, v)) \times R_d \quad (5)$$

Here,  $I'(u, v)$  is the scale normalized texture value in the range  $[0, 1]$  of the mapped  $(u, v)$  texture from the 2D calibration pattern on the vertex  $v$ , and  $R_d$  is the maximum vertical ridge displacement which is set to 0.22 mm in our experiments<sup>6</sup>.

## 2.5 Postprocessing 3D finger surface

The engraved  $S_{OF}$  and  $S_{OR}$  are then combined together to recreate the outer finger surface  $S'_O$ . The outer finger surface  $S'_O$  is then stitched together with the retained original finger surface  $S_O$  to create a continuous watertight 3D shell  $S_W$  ready for 3D printing. For doing this, the boundary of the two meshes  $S'_O$  and the  $S_O$  is first computed. Triangles are then synthetically generated to connect the two boundaries to create a continuous shell

6. The average ridge height on an adult human fingerprint is about 0.06 mm; however we set  $R_d$  to 0.22 mm empirically due to limitation of the 3D printer resolution used for fabricating the targets.

(see Fig. 7). This continuous watertight shell is basically the 3D target  $A$  in electronic form.

## 2.6 3D printing

We use a state-of-the-art 3D printer (Stratasys Objet350 Connex) that has  $X$  and  $Y$  resolution of 600 dpi and  $Z$  resolution of 1600 dpi for fabricating the 3D targets with rubber-like materials. This printer is based on PolyJet printing technology which slices a 3D model into horizontal layers, and then prints the model layer by layer. The 3D targets are printed in high speed mode wherein they are sliced into 30 micrometer layers during the printing process. Note that the printer does not support printing the target with rubber-like materials in the high resolution mode which allows for even finer 16 micrometer layer slicing. However, we found that 30 micrometer slicing suffices with ridge displacement  $R_d$  of 0.22 mm. Note that in the high speed mode, the time taken to fabricate one 3D target using the printer is around 1.5 hrs.

Two different rubber-like materials, TangoBlackPlus FLX980 [31], and FLX 9840-DM [32] (a digital material synthesized in the printer using a rubber-like material and a rigid material) are used for printing the 3D targets. These materials are specifically selected because they are similar in hardness and elasticity to the human finger skin (see Table 2).

While printing the 3D targets, the printer uses a support material to prevent the models being fabricated from breaking. As a result, once the targets are printed they need to be cleaned to remove the support material. Although manual cleaning can remove most of the support material, often residue of the support material is left even after careful manual cleaning. Therefore, a high pressure water jet is used to clean the 3D printed models.



TABLE 3

Similarity scores between the captured snapshots of the 3D electronic targets in Meshlab and the fingerprint images used in their synthesis. Five fingerprints from the NIST SD4 were used. Verifinger 6.3 SDK was used for comparing fingerprints. The similarity threshold @FAR = 0.01% is 33.

| Fingerprint | S0005 | S0010 | S0017 | S0083 | S0096 |
|-------------|-------|-------|-------|-------|-------|
| scores      | 171   | 378   | 212   | 116   | 106   |

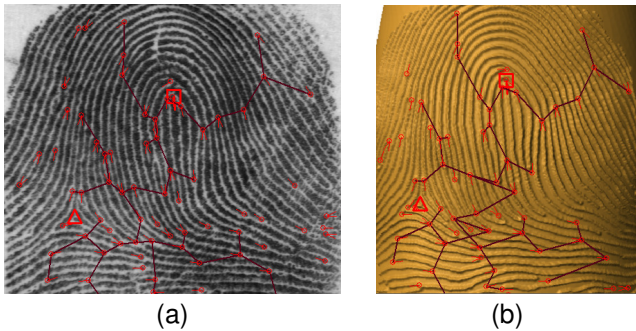


Fig. 8. Feature comparison (minutiae, core and delta shown here) between (a) rolled fingerprint image (S0083) from the NIST SD4, and (b) snapshot of the electronic 3D target synthesized using the fingerprint in (a) using Verifinger 6.3 SDK. Similarity score of 116 is obtained between (a) and (b).

### 3 FIDELITY OF 3D TARGET SYNTHESIS

Given that we synthesize 3D targets for evaluating fingerprint readers, it is important to assess if the synthesized targets are adequate in terms of their utility for this purpose. To determine the fidelity of 3D target synthesis, we evaluate the targets to determine if the

- features present in the 2D pattern,  $I$ , are preserved during projection to 3D to create the electronic (virtual) 3D target,
- features engraved on the electronic 3D finger surface are preserved after fabrication of the physical 3D target,
- features present in the 2D pattern,  $I$ , are preserved on the physical 3D target, and
- intra-class variability between the captured impressions of the 3D target using fingerprint readers is minimal.

Five different rolled fingerprint impressions from the NIST Special Database 4 (NIST SD4) [33] are projected onto a 3D finger surface to synthesize 3D targets. The targets are fabricated with each of the two fabrication materials using a state-of-the-art 3D printer (see Section 2.6). Three optical fingerprint readers (500/1000 ppi)

TABLE 4

Similarity scores between the captured snapshots of the 3D electronic targets and the captured impressions of the physical 3D targets fabricated with TangoBlackPlus FLX980 and FLX 9840-DM using the three optical readers. Five fingerprints from the NIST SD4 were used. Verifinger 6.3 SDK was used for comparing fingerprints. The similarity threshold @FAR = 0.01% is 33.

| TangoBlackPlus FLX980 |                |                 |                 |
|-----------------------|----------------|-----------------|-----------------|
| Fingerprint           | OR 1 (500 ppi) | OR 2 (1000 ppi) | OR 3 (1000 ppi) |
| S0005                 | 191            | 215             | 203             |
| S0010                 | 153            | 173             | 140             |
| S0017                 | 114            | 164             | 155             |
| S0083                 | 315            | 497             | 498             |
| S0096                 | 110            | 162             | 183             |

| FLX 9840-DM |                |                 |                 |
|-------------|----------------|-----------------|-----------------|
| Fingerprint | OR 1 (500 ppi) | OR 2 (1000 ppi) | OR 3 (1000 ppi) |
| S0005       | 194            | 164             | 192             |
| S0010       | 158            | 159             | 168             |
| S0017       | 129            | 165             | 162             |
| S0083       | 353            | 431             | 554             |
| S0096       | 107            | 152             | 164             |

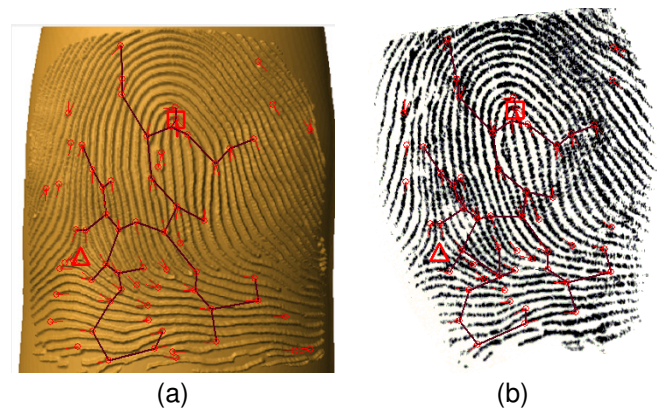


Fig. 9. Feature comparison (minutiae, core and delta shown here) between (a) snapshot of the electronic 3D target synthesized using the fingerprint S0083 in NIST SD4, and (b) the captured impression by optical reader 2 (1000 ppi) of the physical 3D target fabricated with TangoBlackPlus FLX-980 using Verifinger 6.3 SDK. Similarity score of 497 is obtained between (a) and (b).

are used for imaging the 3D targets<sup>7</sup>. A commercial fingerprint SDK [17] is used for conducting all matching experiments.

7. Capacitive fingerprint readers could not be used because state-of-the-art 3D printers currently do not allow printing objects using conductive materials. However, capacitive readers could be used provided that the targets are fabricated using conductive materials. We are currently exploring the possibility of using alternative fabrication methods.

TABLE 5

Similarity scores between the captured impressions of the 3D targets fabricated with TangoBlackPlus FLX980 and FLX 9840-DM using the three optical readers and the fingerprint impressions used in their synthesis. Five fingerprints from NIST SD4 were used. Verifinger 6.3 SDK was used for comparing the impressions. The similarity threshold @FAR = 0.01% is 33.

| TangoBlackPlus FLX980 |                |                 |                 |
|-----------------------|----------------|-----------------|-----------------|
| Fingerprint           | OR 1 (500 ppi) | OR 2 (1000 ppi) | OR 3 (1000 ppi) |
| S0005                 | 105            | 68              | 71              |
| S0010                 | 90             | 77              | 78              |
| S0017                 | 89             | 83              | 74              |
| S0083                 | 96             | 128             | 123             |
| S0096                 | 101            | 98              | 74              |

| FLX 9840-DM |                |                 |                 |
|-------------|----------------|-----------------|-----------------|
| Fingerprint | OR 1 (500 ppi) | OR 2 (1000 ppi) | OR 3 (1000 ppi) |
| S0005       | 80             | 66              | 65              |
| S0010       | 80             | 104             | 80              |
| S0017       | 108            | 96              | 89              |
| S0083       | 110            | 120             | 120             |
| S0096       | 75             | 81              | 71              |

TABLE 6

Range of similarity scores for pairwise comparisons between five impressions of the 3D targets fabricated with TangoBlackPlus FLX980 and FLX 9840-DM captured by the three optical readers. Five fingerprints from NIST SD4 were used in their synthesis. Verifinger 6.3 SDK was used for comparing the impressions. The similarity threshold @FAR = 0.01% is 33.

| TangoBlackPlus FLX980 |                |                 |                 |
|-----------------------|----------------|-----------------|-----------------|
| Fingerprint           | OR 1 (500 ppi) | OR 2 (1000 ppi) | OR 3 (1000 ppi) |
| S0005                 | 581-1370       | 902-1643        | 846-1394        |
| S0010                 | 696-1656       | 534-1463        | 819-1194        |
| S0017                 | 900-1171       | 945-1478        | 515-1284        |
| S0083                 | 831-1935       | 1466-1836       | 1364-1746       |
| S0096                 | 707-1170       | 812-1392        | 984-1287        |

| FLX 9840-DM |                |                 |                 |
|-------------|----------------|-----------------|-----------------|
| Fingerprint | OR 1 (500 ppi) | OR 2 (1000 ppi) | OR 3 (1000 ppi) |
| S0005       | 417-1514       | 990-1439        | 890-1494        |
| S0010       | 659-1196       | 906-1292        | 1043-1355       |
| S0017       | 1016-1937      | 1088-1482       | 1326-1571       |
| S0083       | 810-1520       | 1193-1547       | 1356-1757       |
| S0096       | 459-1062       | 1352-1496       | 1127-1511       |

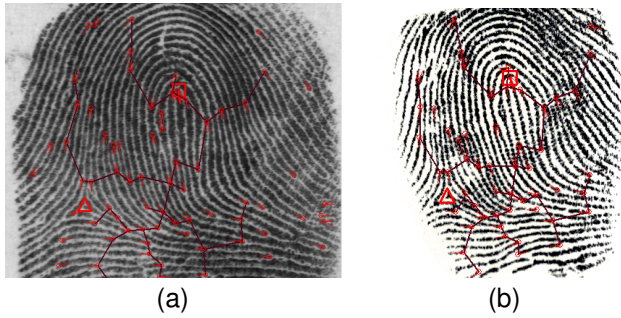


Fig. 10. Feature comparison (minutiae, core and delta shown here) between (a) rolled fingerprint image (S0083) from the NIST SD4, and (b) the captured image using optical reader 2 (1000 ppi) of the 3D target synthesized using the fingerprint in (a) and fabricated with TangoBlackPlus FLX980 using Verifinger 6.3 SDK. Similarity score of 128 is obtained between (a) and (b).

### 3.1 Fidelity of 2D pattern features during projection to 3D surface

Each electronic 3D target is previewed in the 3D mesh processing software Meshlab [34], and its frontal snapshot is taken. The captured snapshot of the electronic 3D target is rescaled manually to the same scale as the original 2D fingerprint images used during the synthesis of the target. The rescaled snapshot images of the electronic 3D target is matched to the original 2D fingerprint image using the commercial fingerprint SDK.

Fig. 8 shows a sample fingerprint image from the NIST SD4 and the snapshot of an electronic 3D target. The

features extracted and matched using the commercial fingerprint SDK are marked on the two images. Table 3 shows the obtained similarity scores for the experiment. All similarity scores are significantly above the verification score threshold of 33 (@FAR = 0.01%) for NIST SD4. It can, thus, be inferred that the features present in the 2D fingerprint image are preserved during the synthesis of the electronic 3D target.

### 3.2 Fidelity of the engraved features on the 3D surface after 3D printing

The snapshot of an electronic 3D target is matched to captured impression of the physical 3D target using the three optical readers for each of the ten 3D targets. Fig. 9 shows feature comparison obtained using the commercial fingerprint SDK between the snapshot of one electronic target and its captured impression using one optical reader. Table 4 shows the obtained scores for this experiment. Notice that the similarity scores are significantly above the verification threshold score of 33 (@FAR = 0.01%) for all targets. This demonstrates the fidelity of features engraved on the 3D surface after 3D printing.

### 3.3 End-to-end fidelity of 2D pattern features after 3D printing

Table 5 shows the similarity scores obtained on matching the captured impressions of the 3D target to the original fingerprint for each of the five 3D targets printed with the two materials and imaged using the three readers. Fig. 10 shows feature comparison between the fingerprint

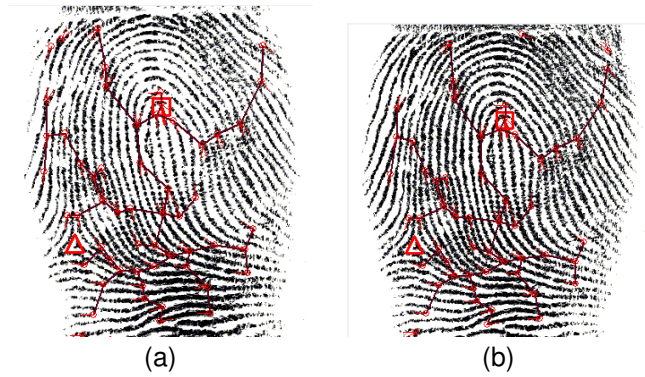


Fig. 11. Feature comparison (minutiae, core and delta shown here) between two captured impressions (a) and (b) using optical reader 2 (1000 ppi) of a 3D target fabricated with TangoBlackPlus FLX980 using Verifinger 6.3 SDK. The 3D target was synthesized using a rolled fingerprint image (S0083) in NIST SD4. Similarity score of 1592 is obtained between (a) and (b).

image and captured impressions of the synthesized 3D target using the commercial fingerprint SDK. The key observations and inferences based on this experiment are:

- The captured images of the 3D targets using the three optical readers can be successfully matched to the original fingerprint images used for synthesizing the targets with high confidence. This is because all similarity scores (see Table 5) are significantly above the verification threshold score of 33 (@FAR = 0.01%) computed for the NIST SD4.
- Because the captured images of the 3D targets can be successfully matched to the original fingerprint images (@FAR = 0.01%), it can be inferred that the salient features present in the 2D pattern are preserved during the fabrication of the physical 3D target.

### 3.4 Intra-class variability between 3D target impressions

Five different impressions of each of the ten 3D targets are captured using each of the three optical readers. Pair-wise comparisons between the five impressions obtained from a reader are performed using the commercial fingerprint SDK. Fig. 11 shows the extracted and matched features by the fingerprint SDK between two impressions of a 3D target captured using the three readers. Table 6 shows the range of similarity scores obtained for this experiment. It is observed that the similarity scores obtained are significantly higher than the verification threshold, thereby, indicating that the intra-class variability between multiple different captured impressions of the 3D target is minimal. In other words, different impressions of the 3D target are fairly consistent.

TABLE 7  
Mean ( $\mu$ ) and std. deviation ( $\sigma$ ) of computed center-to-center spacing in the acquired images of the three test targets using the three optical readers. (original grating spacing = 10 pixels)

| Test pattern | OR 1 (500 ppi)              | OR 2 (1000 ppi)             | OR 3 (1000 ppi)             |
|--------------|-----------------------------|-----------------------------|-----------------------------|
| Horizontal   | $\mu = 9.04, \sigma = 0.06$ | $\mu = 9.18, \sigma = 0.07$ | $\mu = 9.05, \sigma = 0.05$ |
| Vertical     | $\mu = 9.51, \sigma = 0.23$ | $\mu = 9.57, \sigma = 0.07$ | $\mu = 9.46, \sigma = 0.09$ |
| Circular     | $\mu = 9.80, \sigma = 0.31$ | $\mu = 9.62, \sigma = 0.07$ | $\mu = 9.59, \sigma = 0.08$ |

## 4 EVALUATING FINGERPRINT READERS USING 3D TARGETS

For evaluating the fingerprint readers, three different 3D targets are created by projecting synthetically generated 2D test patterns: (i) horizontal, (ii) vertical, and (iii) circular gratings with a fixed center-to-center spacing of 10 pixels. Ten different impressions of each of the three targets are captured using the three optical readers. Center-to-center spacing is then measured in each of the captured impressions using the method in [35]. Fingerprint readers are subsequently evaluated based on how well the grating spacings on the three targets is recovered by the readers. Figs. 12, 13 and 14 show the three test patterns, the electronic targets generated using the three patterns, and some sample images of the three targets captured using the three optical fingerprint readers.

The average and standard deviation of the observed center-to-center spacings in the captured impressions of the three targets is reported in Table 7. Note that to compensate for the distortion induced during 2D to 3D projection of the 2D pattern, the ratio of the Euclidean distance on the pattern to Geodesic distance (0.94) on the 3D finger surface is factored into spacing computations. Following are some observations based on this experiment:

- The observed spacing, on average, is greater than 9 pixels in the captured images of all three targets using the three readers. The three readers, therefore, image the three targets with accuracies greater than 90%.
- The spacing in images of the horizontal target is, on average, less than those of the vertical target for all three optical readers. In other words, the readers better capture vertical spacings than horizontal spacings.
- The 500 ppi optical reader (OR 1) has a greater variation in the observed spacings in the captured images compared to the 1000 ppi readers (OR 2 and OR 3). This is because OR 1 images a smaller portion of the targets, and depending on how the user places the finger on the platen, the captured portion of the target differs between different impressions.

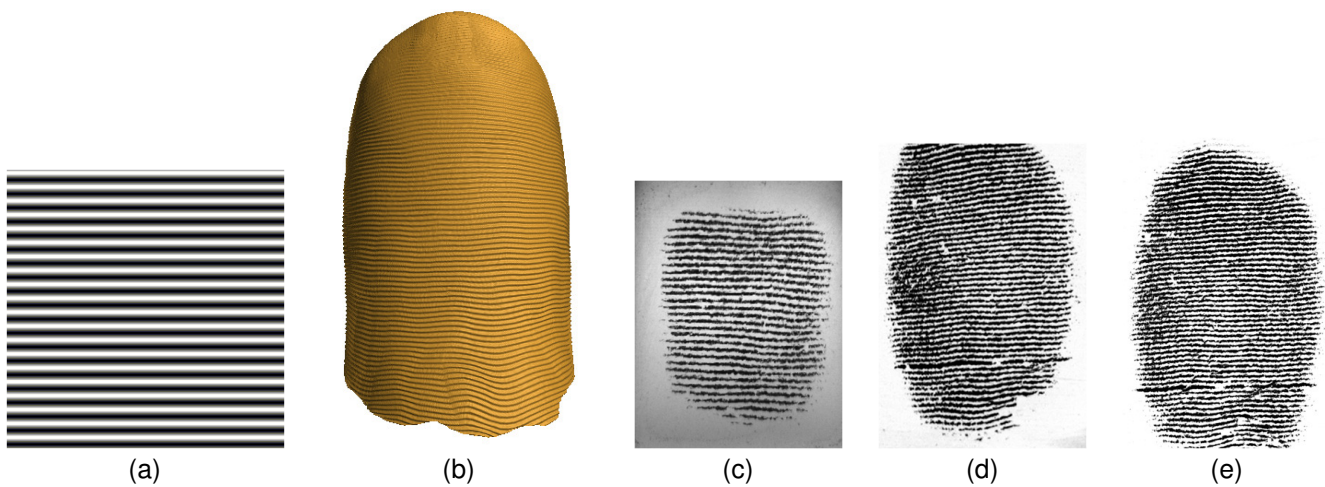


Fig. 12. Evaluating fingerprint readers using a 3D target synthesized from a horizontal sine grating. (a) Horizontal sine grating (10 pixels); (b) electronic 3D target synthesized using (a); (c),(d) and (e) are sample impressions of the fabricated target captured using optical readers 1, 2 and 3, respectively.

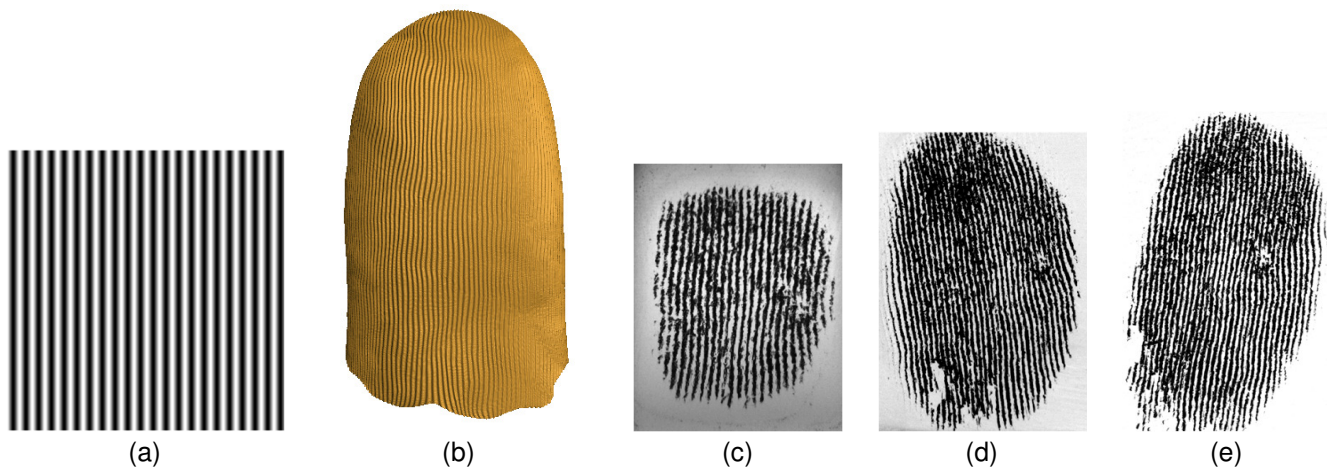


Fig. 13. Evaluating fingerprint readers using a 3D target synthesized from a vertical sine grating. (a) Vertical sine grating (10 pixels); (b) electronic 3D target synthesized using (a); (c),(d) and (e) are sample impressions of the fabricated target captured using optical readers 1, 2 and 3, respectively.

## 5 CONCLUSIONS AND ONGOING WORK

Calibration of fingerprint readers is typically done using 2D/3D targets designed for calibrating imaging devices. These targets are suitable for calibrating the imaging pathway of fingerprint readers. However, they cannot be used for repeatable operational evaluation of fingerprint readers. In this research, we have designed and fabricated wearable 3D targets which can be worn on a finger, placed on the reader platen, and imaged analogous to operational setting for evaluating fingerprint readers. The 3D targets are created by projecting 2D calibration patterns of known characteristics (e.g. sine gratings of known spacings) onto a generic 3D finger surface, and are fabricated using a state-of-the-art 3D printer with

materials similar in hardness and elasticity to the human finger skin. Our experimental results show that (i) our 3D targets can be imaged by three different commercial optical fingerprint readers, (ii) features present in the 2D calibration patterns are generally preserved during the projection of the 2D pattern to synthesize electronic 3D targets, (iii) features engraved on the electronic 3D targets are generally preserved after fabricating physical 3D targets, and (iv) the intra-class variability between multiple images of the same 3D target captured using three different optical fingerprint readers is small. Experiments are also conducted to evaluate the three optical readers using the fabricated 3D targets.

We are currently investigating alternative methods to fabricate the 3D targets with higher precision. We are

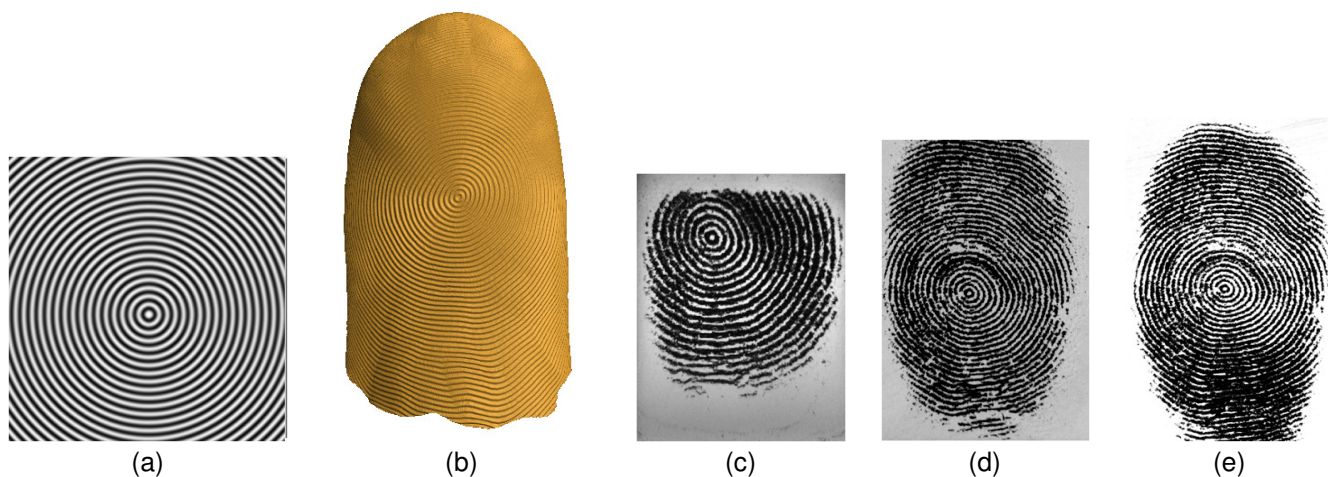


Fig. 14. Evaluating fingerprint readers using a 3D target synthesized from a circular sine grating. (a) Circular sine grating (10 pixels); (b) electronic 3D target synthesized using (a); (c), (d) and (e) are sample impressions of the fabricated target captured using optical readers 1, 2 and 3, respectively.

also investigating the possibility of using materials with similar optical properties and conductivity to the human finger skin to fabricate 3D targets for evaluating both optical and capacitive fingerprint readers. In future, we plan to simulate the effects of dry and worn fingers using 3D targets with different depths of engravings to further study the imaging capabilities of different readers.

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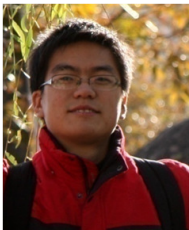
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